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A COMPUTER PROGRAM FOR BACKSCATTER BY TARGETS COMPOSED OF CONES, CYLINDERS, AND DISKS - 2430-5



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FOREWORD

This report, OSURF report number 2430-5, was prepared by The Ohio State University ElectroScience Laboratory, Department of Electrical Engineering, 1320 Kinnear Road, Columbus, Ohio. Research was conducted under Contract F 19628-67-C-0308. Lt. Nyman was the Electronic Systems Division Program Monitor for this research.

This technical report has been reviewed and is approved.

EERNARD J. FILLIATREAULT Contracting Officer Space Defense & Command Systems Program Office

ABSTRACT

This report describes a computer program for determining the backscattered fields of a conducting body of revolution composed of sections of cones and cylinders. The target may be closed at one or both ends with circular disks. The target may have as many as 20 sections, and the program can readily be modified to handle a larger number. The backscattered field for E_θ or E_φ polarization is computed using wedge diffraction theory and geometrical optics. The computed results are in good agreement with experimental measurements for cones, cylinders, double cones, and conically capped cylinders.

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A COMPUTER PROGRAM FOR BACKSCATTER BY TARGETS COMPOSED OF CONES, CYLINDERS, AND DISKS

INTRODUCTION

A computer program, which computes the backscattered field of a body of revolution composed of cones, frustums, cylinders, and disks is given in Appendix I. This program is coded in Fortran IV and the cards are numbered consecutively in columns 76-80. This program has been tested for cones, cylinders, frustums, conically capped cylinders, and double cones, for E θ polarization of the incident and scattered fields. The results of these tests are presented in Reference 1. The theoretical basis for this program is described in References 1 and 2.

The function of this program is to compute the backscattered field as a function of aspect angle and/or frequency for a given target. This is accomplished by reading and storing the target description, identifying the regions of aspect angle corresponding to axial and specular directions, and applying the appropriate geometrical theory of diffraction solutions to calculate the scattered fields. In the form presented here the angular pattern for a given target and frequency is computed. Modification of the program to compute a frequency curve for a given target and aspect angle is straightforward.

TARGET DESCRIPTION

The target shape is described in cylindrical coordinates by the second degree equation

(1)
$$F(\rho,z) = A_1 \rho^2 + A_2 z^2 + A_3 \rho z + A_4 z + A_5 \rho + A_6 = 0.$$

As this program is written to handle only targets composed of cones, frustums, cylinders and disks, the description of the profile of the target is that of a straight line segment, and may be expressed as

(2)
$$F(\rho, z) = A_4 z + A_5 \rho + A_6 = 0$$

where $A_1 = A_2 = A_3 = 0$. In addition to Eq. (2) the boundaries of each section of the target must be specified. That is, within each section of

the target the profile is specified by a set of constants A_4 , A_5 , A_6 . The next section is described by a new set of constants and so forth. As an example consider the target shown in Fig. 2. This target is composed of a cone, a cylinder, and a disk, and is a three section target. Thus a set of constants must be specified for each section and the angular boundaries of the sections specified. Figure 1 gives the relations by which the constants may be determined for each surface. The computer format for this input data will be discussed below.

If Eq. (1) is used to describe the target, i.e., any of the constants A_1 , A_2 A_3 non-zero, this program will compute the scattered field due to the wedge type discontinuities on the target but will not calculate the correct total scattered field. This is because there is no provision in this program to calculate the geometrical optics field of a doubly curved surface. A calculation of this geometrical optics field is included in the creeping wave computer program.³

WEDGE DIFFRACTION COMPUTER PROGRAM

Referring to the computer program listing shown in Appendix I, the function of the significant sections of the program will be discussed. The card numbers associated with each section will be specified. This discussion, together with the comment cards included in the program listing, is intended to give sufficient information about the program to enable a qualified programmer to both use and modify the program. Statements which are in common use in Fortran IV such as DIMENSION, COMPLEX, and FORMAT statements will not be discussed as it is assumed that the reader has a knowledge of Fortran IV.

The COMMON declaration (0006) is used to store the constants required in Eq. (2) in the common block labelled / DATA/. This common block is used in conjunction with the unlabelled common block to transfer a particular set of constants Al(I) to A6(I) into the unlabelled common regions shared by the subroutines. This provision reduces the number of calling variables required by each subroutine.

The READ (0030-0040) statements in this block of statements read the required data and provision is also made to write out this data for the purpose of identification.

The statements 0041-0045 initialize constants which are required in the calculations.

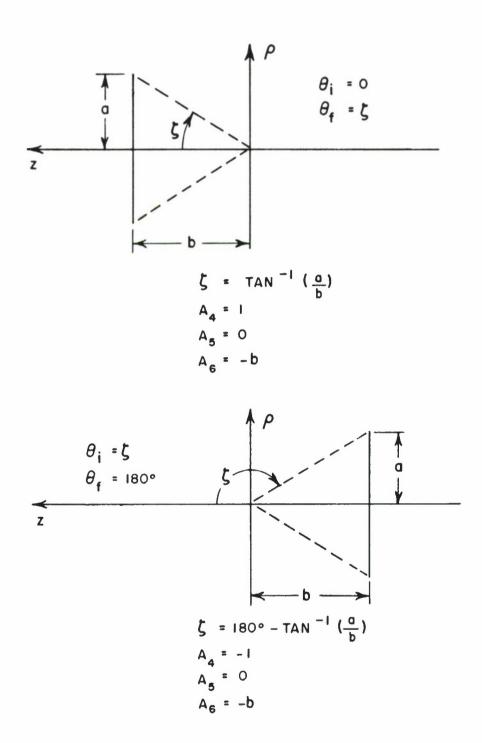


Fig. 1(a). Straight line segments and their corresponding analytic description.

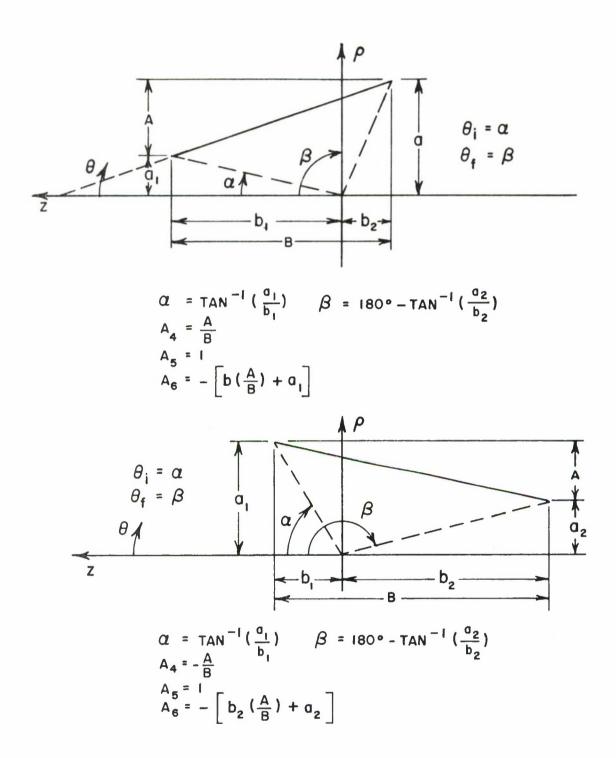


Fig. 1(b). Straight line segments and their corresponding analytic description.

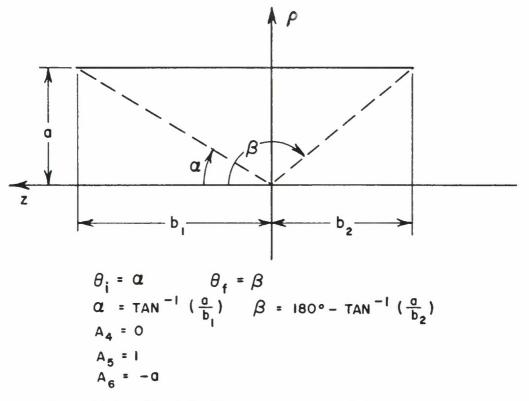


Fig. 1(c). Straight line segments and their corresponding analytic description.

The next block of statements (0046 - 0108) identifies the geometrical properties of the target. The function of this section may be described by consideration of a particular target. Figure 2 shows a particular target composed of a cone-cylinder-disk. The geometrical properties of interest are the locations of the wedges, the wedge angles WA(IW), the specular directions THSX(IW), and the length of the specular line FLSX(IW). This task is accomplished by examining the normal vectors (VNX, VNY, VNZ) of the adjoining surfaces at the junction between two sections. The wedge angle is then obtained from the scalar product of the normal vectors, the specular direction is determined by checking for parallel normals at the ends of each section, and the length of the specular line is obtained using the law of cosines.

The next block of statements (0109 - 0110) remove the redundancy in specular angle which can occur when the z-axis is a specular direction. For example, in the case of a closed cylinder the directions θ = 0°, 180° are specular directions. In a subsequent test for a specular region in (0190 - 0196) the sine of the specular angle is taken. As the sine is periodic in 180° care must be taken that the shadowed specular region

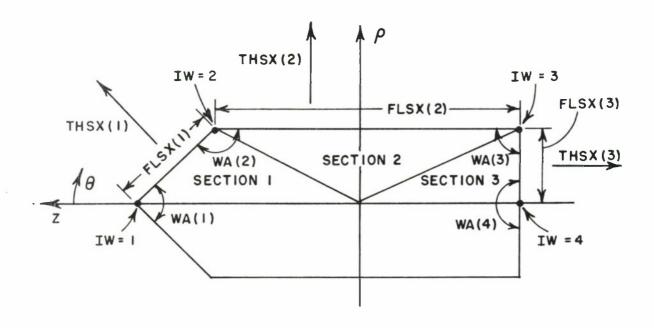


Fig. 2. A three section target-the cone-cylinder-disk.

is not included in evaluating the scattered field. This is accomplished by setting the specular angles 0° and 180° equal to 360°. These specular directions on the axis may then be evaluated using the solution for the axial caustic given in Ref. 1, and located at (0242 - 0266) in this program.

The statements (0111 - 0115) convert the computed wedge angles WA(IWD) to the parameter FN(IWD) required for the wedge diffraction coefficient, where IWD is the number of the particular wedge.

Having identified the required geometrical properties of the target the scattered field must now be computed. Thus the iteration for the incidence angle THT is set up (0116 - 0117) and the DO loop entered (0118). The incidence angle is incremented and the propagation vector of the incident wave is computed (0119 - 0124). Next, the total field is initialized. Then a DO loop is entered (0128) in which the total scattered field is to be obtained by summation of the individual contributions. First the location of the wedge ID is computed (0129 - 0135). Next the test parameter BESAR for the axial solution region is computed. At this point a transfer to the solution for a tip scattered field is made if ID = NWD (0137). A determination is now made whether the points on the

wedge ID at ϕ = 0°, 180° are illuminated or shadowed by calling the subroutine WILLY (0138 - 0143). The COMMON block is now reset (0144), having been used in the previous test, and the angle between the incident ray and the "side" of the wedge ID is computed (0145 - 0177). The phase of the backscattered field of the ϕ = 0°, 180° points on the wedge ID is calculated by the subroutine PHASE. Having completed these calculations we now move to the computation of the scattered field due to the "wedge" ID.

The first step in the field calculation is a test (0185 - 0189) to determine if the incident angle THT is in a region for which the axial solution must be used. This region is bounded by the angle corresponding to the first null of the first order Bessel function $J_1(2ka\sin\theta)$. If so a transfer is made to the axial solution. Next (0190 - 0197) a test is made to determine whether the incidence angle is within a region about a specular direction specified by the first null of the $\sin(x)/x$ function. If so a transfer to the specular solution is made. It is noted that as this test is made after the test for the axial region the axial solution has precedence. At this point a transfer to the solution for a tip scattered field is made if ID = 1. Locating this provision after the axial and specular region test insures that the specular region THSX(1) indicated in Fig. 2 will be included.

Having tested for regions where a special solution is required, the scattered field due to the wedge discontinuity is now computed (0201 - 0210), and added to obtain the total field. A transfer to the end of the DO loop is then made.

The solution for the specular field using the $\sin(x)/x$ formulation given in Ref. 2, is computed in 0211 - 0238. Again this field is added to obtain the total field, and upon completion transfers to the end of the DO loop.

The solution for the axially scattered fields given in Ref. 2 is computed in 0239 - 0272. Again this contribution is added to obtain the total field, and a transfer is made to the end of the DO loop.

The tip scattered fields are computed in 0273 - 0297 using the physical optics solution for the field scattered by an infinite conducting cone. Again this contribution is added to obtain the total scattered field.

Statement 301 (0297) is the end of the range of the DO loop over the number of wedges. Thus at this point the contribution of the wedge (ID) to the total field has been computed and added to the scattered field. At the termination of the DO loop the total backscattered field EDTOT due to all contributions has been computed. Next the backscattered field and the echo area for the incident angle THT are written (0298 - 0305). After the loop on incidence angle is completed the program is terminated (0306 - 0308).

SUBROUTINES AND FUNCTIONS

Subroutine FNORM(FNVX, FNVY, FNVZ, R, THT, PHI) 0309 - 0331

This subroutine computes the normal vector (FNVX, FNVY, FNVZ) to the surface for the section whose description is in the unlabelled COMMON region. The spherical coordinates of the point at which the normal is computed are R, THT and PHI.

Subroutine FCOMM(I) 0332 - 0343

This subroutine shifts the constants describing the section I from the /DATA/COMMON into unlabelled COMMON.

Function RAD(THT) 0344 - 0363

This function calculates the distance from the origin to the surface at the angle THT. The constants describing the surface are stored in unlabelled COMMON.

Subroutine WILLY(FWI, THTI, PHI, THIN, PHIN)

This subroutine determines whether the incident wave specified by THIN, PHIN = 0., π illuminates the wedge at location THTI, PHI. If the wedge is illuminated FWI is set equal to 1., if shadowed FWI is set equal to zero.

Subroutine CROSS(X, Y, Z, A1, A2, A3, B1, B2, B3) 0384 - 0390

This subroutine computes the cross product \overrightarrow{AXB} and returns the answer in (X, Y, Z).

Function PHASE(THTI, PHII, THTB, PHIB, RB, FK) 0391 - 0400

This function calculates the phase of the backscattered field for an incident (and scattering) direction given by THTI, PHII = $0.,\pi$, for the wedge location RB, THTB, PHIB = $0.,\pi$, with a propagation constant FK.

Function SINXX(Y) 0401 - 0408

This function computes $\sin(y)/y$.

Function DIFF1(FN, PHI, FK, BETA) 0409 - 0439

This function calculates the plane wave diffraction coefficient given in Refs. 1 and 2. FN is the wedge parameter, PHI the angular argument, FK the propagation constant, and BETA the half angle of the diffraction cone.

Function BESL0(X) 0440 - 0465

This function computes the zero order Bessel function $J_{O}(x)$.

Function BESL1(X) 0466 - 0491

This function computes the first order Bessel function $J_1(x)$.

Function BESL2(X) 0492 - 0501

This function computes the second order Bessel function J₂(x).

INPUT DATA

A typical set of data cards is shown in Appendix II. The order of the cards is as follows:

Card #1 This card specifies in format (115) the number of cases to be run.

- Card #2 This card specifies the number of sections of the target, in format (115).
- Card #3 This card specifies, in order, the wavelength of the incident radiation, the starting incidence angle, the final incidence angle, the increment in angle, and the polarization factor. The wavelength is in meters, the angles in degrees, and the polarization factor is (± 1 .) for E_{θ} polarization or (-1.) for E_{φ} polarization. The format is (5F10.5).
- Next N cards (N=number of target sections). These cards specify in order, the initial and final angular boundaries of the section (in radians), and the constants A₁...A₆. The format is (8F10.5).

If the number on card number l is different from l, the cards #2 to (#3+N) are repeated. This is necessary if any of the following options are desired.

- 1. A change in incidence angle range.
- 2. A change in wavelength.
- 3. A change in polarization.
- 4. A change in target.

It is also possible to re-write the control statements in the program to provide more versatility in the control, that is, to provide for automatic looping over wavelength, or polarization. The form presented here is convenient as most experimental data is taken in the form of an echo area pattern, rather than as echo area versus frequency. A flow diagram of the program is given in Appendix IV.

CONCLUSIONS

This report is not intended to completely specify each detail of the computer program. It is intended to provide information about the program which is necessary to the use or modification of the program. The accuracy of the program has been tested for the case of E_{θ} (parallel) polarization as reported in Ref. 1. Tests for E_{φ} (perpendicular) polarization have not been completed, but some results are given in Appendix III.

APPENDIX I COMPUTER PROGRAM

```
ROLBI
$EXECUTE
                                                                                   0000
                                                                                   1000
                GO . MAP
$18J08
$18FTC WEDGD
                LIST . NODECK
                                                                                   0002
      COMPLEX EDIOT, PHASE, PHWU, PHWL, WDU, WDL, EDU, EDL, ESX, EBESS, ETIP
                                                                                   0003
       COMPLEX DIFFI.WBS.PBESS
                                                                                   0004
      COMPLEX WBSP . WBSM
                                                                                   0005
      COMMON RAI . RA3 . R81 . RA9 . RAI 0 . RA11/DATA/ARI (20) . AR3 (20) . BR1 (20) . AR9 (
                                                                                   0006
     (20) + AR10(20) + ARI1(20)
                                                                                   0007
      DIMENSION THSX(20) + FLSX(20) + THTI(20) + THTF(20)
                                                                                   0008
      DIMENSION VNX(20). VNY(20). VNZ(20)
                                                                                   0009
      DIMENSION WA(21) +FN(21)
                                                                                   0010
      FORMAT(115)
 1
                                                                                   0011
      FORMAT (5F10.5)
                                                                                   0012
 3
      FORMAT (8F13.5)
                                                                                   0013
      FORMAT (3F15.8)
                                                                                   0014
 4
 5
      FORMAT(5H RW1=F15.8.5H RW2=F15.8)
                                                                                   0015
      FORMAT (6H FLSX=F15.8.6H THSX=F15.8)
 6
                                                                                   0016
      FORMAT (5H WDU=2F15.8.5H WDL=2F15.8.5H RDF=F15.8)
                                                                                   0017
      FORMAT (4F15.8)
                                                                                   0018
  9
      FORMAT(1FI5.8)
                                                                                   0019
     FORMAT (6F15.8)
                                                                                   0020
  10
      FORMAT(6H THTD=F15.8.5H ESX=2F15.8)
                                                                                   1500
  1 1
      FORMAT(6H THTD=F15.8.7H EBESS=2F15.8)
                                                                                   0022
 12
      FORMAT (6H STTI=F15.8)
                                                                                   0023
 13
 14
      FORMAT(6H ARSX=F15.8)
                                                                                   0024
 15
      FORMAT (6H PSIU=F15.8.6H PSIL=F15.8)
                                                                                   0025
      FORMAT(6H FWIU=F15.8.6H FWIL=F15.8)
                                                                                   0026
 16
  17 FORMAT(6H THTW=F15.8.4H RW=F15.8.4H AW=F15.8.4H ZW=F15.8)
                                                                                   0027
      FORMAT(27H PERPENDICULAR POLARIZATION)
                                                                                   0028
  18
      FORMAT(22H PARALLEL POLARIZATION)
                                                                                   0029
      READ(5.1) NCS
                                                                                   0030
      DO 600 NCSI=1+NCS+1
                                                                                   0031
                                                                                   0032
      READ (5.1) N
      READ (5.2) WAVE . THTS . THTE . DTHT . POL
                                                                                   0033
      WRITE(6.2)WAVE.THTS.THTE.DTHT.POL
                                                                                   0034
      IF(POL.LT.O.) WRITE(6.18)
                                                                                   0035
                                                                                   0036
      IF(POL.GT.O.) WRITE(6.19)
      READ(5.3)(THTI(1RD).THTF(IRD).AR1(1RD).AR3(IRD).8RI(IRD).AR9(IRD).
                                                                                   0037
     CARIO(IRD) + AR1I(IRD) + IRD=1+N)
                                                                                   0038
      WRITE(6.3)(THTI(J).THTF(J).AR1(J).AR3(J).BR1(J).AR9(J).AR10(J).AR1
                                                                                   0039
     C1(J) • J=1 • N)
                                                                                   0040
      PI=3.1415927
                                                                                   004 I
                                                                                   0042
      TP=2.*PI
                                                                                   0043
      P12=P1/2.
                                                                                   0044
       FK=TP/WAVE
                                                                                   0045
      DEGRAD=0.01745329
                                                                                   0046
      WEDGE DETERMINATION
C
      NUMBER OF TARGET SECTIONS=N
                                                                                   0047
C
                                                                                   0048
      CLOSED TARGET ASSUMED
                                                                                   0049
      NWD=N+I
                                                                                   0050
      DLARGE = 0 .
                                                                                   0051
      DIA=0.
      TCT=0.90
                                                                                   0052
                                                                                   0053
      DO 201 IW=1.N.I
                                                                                   0.054
      THSX(IW) = TP
                                                                                   0055
      FLSX(IW)=0.
                                                                                   0056
      THT1=THTI(IW)
                                                                                   0057
      THT2=THTF(IW)
                                                                                   0058
      CALL FCOMM(IW)
                                                                                   0059
      RW1=RAD(THT1)
                                                                                   0060
      RW2=RAD(THT2)
      CALL FNORM(FXI.FY1.FZ1.RW1.THTI.O.)
                                                                                   0061
      CALL FNORM(FX2, FY2, FZ2, RW2, THT2, 0.)
                                                                                   0062
                                                                                   0063
      IF(IW.EQ.1) GO TO 202
```

```
IW1 = IW - 1
                                                                                 0064
      THT3=THTF(IW1)
                                                                                 0065
      CALL FCOMM(IW1)
                                                                                 0066
      RW3=RAD(THT3)
                                                                                 0067
      CALL FNORM(FX3.FY3.FZ3.RW3.THT3.0.)
                                                                                 0068
      SPRD=FX1*FX3+FY1*FY3+FZ1*FZ3
                                                                                 0069
      VNX(IW)=FX3
                                                                                 0070
      VNY(IW) = FY3
                                                                                 0071
      VNZ(1W)=FZ3
                                                                                 0072
      DANG=ARCOS(ABS(SPRD))
                                                                                 0073
      IF (SPRD.LT.O.) DANG=PI-DANG
                                                                                 0074
      WA(IW)=P1-DANG
                                                                                 0075
      IF(IW.EQ.N)GO TO 203
                                                                                 0076
 207
     CONTINUE
                                                                                 0077
      CHECK FOR SIN(X)/X REGION
                                                                                 0078
      SPX=FX1*FX2+FY1*FY2+FZ1*FZ2
                                                                                 0079
      SPX=ABS(SPX)
                                                                                 0080
      IF (SPX.GT.TCT)GO TO 204
                                                                                 0081
      GO TO 500
                                                                                 0082
 202
    CONTINUE
                                                                                 0083
      CHECK FOR WEDGE ANGLE ON THE END
                                                                                 0084
C
      VNX(I)=FX1
                                                                                 0085
      VNY (1) = FY1
                                                                                 0086
      VNZ(1)=FZ1
                                                                                 0087
      WA(1)=P1-2**ATAN2(FX1*FZ1)
                                                                                 0088
      GO TO 207
                                                                                 0089
 203 CONTINUE
                                                                                 0090
      CHECK FOR WEDGE ANGLE ON THE END
                                                                                 0091
C
      FZ2A=ABS(FZ2)
                                                                                 0092
      VNX(NWD)=FX2
                                                                                 0093
      VNY(NWD)=FY2
                                                                                 0094
      VNZ(NWD) = FZ2
                                                                                 0095
      WA(NWD)=P1-2.*ATAN2(FX2.FZ2A)
                                                                                 0096
      GO TO 207
                                                                                 0097
 204 CONTINUE
                                                                                 0098
      THSX(IW)=ATAN2(FX1+FZ1)
                                                                                 0099
                                                                                 0100
      THHX=THSX(1W)
      IF(IW.GT.1 .AND. ABS(THHX).EQ.O.) THSX(IW)=PI
                                                                                 0101
      FLSX(1W)=SQRT(ABS(RW1*RW1+RW2*RW2-2 •*RW1*RW2*COS(THT2-THT1)))
                                                                                 0102
      GLSX=FLSX(1W)
                                                                                 0103
                                                                                 0104
      WRITE(6.5) RW1.RW2
                                                                                 0105
      WRITE(6.5) THTI.THT2
                                                                                 0106
      WRITE(6.6) GLSX.THHX
 500 CONTINUE
                                                                                 0107
 201 CONTINUE
                                                                                 0108
      1F(THSX(1).LT.0.1) THSX(1)=TP
                                                                                 0109
      IF(ABS(THSX(N)-PI).LT.0.1) THSX(N)=TP
                                                                                 0110
                                                                                 0111
      DO 208 IWD=1 . NWD . 1
                                                                                 0112
      FN(IWD) = (TP-WA(IWD))/PI
                                                                                 0113
      FNWR=FN(IWD)
                                                                                 0114
      WRITE(6.9)FNWR
                                                                                 0115
  208 CONTINUE
                                                                                 0116
      FLOOP=ABS((THTS-THTE)/DTHT)
                                                                                 0117
      LOOP=FLOOP+1 .
                                                                                 0118
      DO 400 LP=1.LOOP.1
      FLP=LP
                                                                                 0119
                                                                                 0120
      THTD=(FLP-1.)*DTHT
                                                                                 0121
      THT=DEGRAD*THTD
                                                                                 0122
      VX = -SIN(THT)
                                                                                 0123
      • C=YV
                                                                                 0124
      VZ = -COS(THT)
                                                                                 0125
C
      PARALLEL POLARIZATION
                                                                                 0126
      EDTOT= (0. . J.)
                                                                                 0127
      IDSX=0
```

```
DO 301 1D=1 .NWD . 1
                                                                                  0128
      THTW=THTI(1D)
                                                                                  0129
      CALL FCOMM(1D)
                                                                                  0130
      1F(1D.EQ.NWD) THTW=THTF(N)
                                                                                  0131
      RW=RAD(THTW)
                                                                                  0132
      AW=RW*SIN(THTW)
                                                                                  0133
      Zw=RW*COS(THTW)
                                                                                  0134
      WRITE(6.17) THTW.RW.AW.ZW
                                                                                  0135
      BESAR=2.*FK*AW
                                                                                  0136
      1F(1D . EQ . NWD) GO TO 305
                                                                                  0137
      IF(THT.LT.P12.AND.1D.GT.1) CALL FCOMM(1D-1)
                                                                                  0138
      CALL WILLY(FW1.THTW.O.THT.O.)
                                                                                  0139
      FW1U=FW1
                                                                                  0140
      CALL WILLY (FW1.THTW.P1.THT.O.)
                                                                                  0141
      FW1L=FW1
                                                                                  0142
      WRITE(6+16) FWIU+FWIL
                                                                                  0143
      CALL FCOMM(1D)
                                                                                  0144
 306
     CONT INUE
                                                                                  0145
      FIND INCIDENCE ANGLE ON WEDGE
C
                                                                                  0146
      INCIDENCE VECTOR VX+VY+VZ
C
                                                                                  0147
      VXM = -VX
                                                                                  0148
      \vee YM = - \vee Y
                                                                                  0149
      VZM=-VZ
                                                                                  0150
      1F(THT.GT.P12) GO TO 309
                                                                                  0151
      SPRD=VXM*VNX(ID)+VZM*VNZ(ID)
                                                                                  0152
      CALL CROSS(BX+BY+BZ+VXM+VYM+VZM+VNX(1D)+VNY(1D)+VNZ(1D))
                                                                                  0153
      DANG=ARCOS(SPRD)
                                                                                  0154
      S1GN=-1 .
                                                                                  0155
      1F(BY.LT.0.) SIGN=1.
                                                                                  0156
      PSIU=P12+SIGN*DANG
                                                                                  0157
      SPRD=-VXM*VNX(1D)+VZM*VNZ(1D)
                                                                                  0158
      CALL CROSS(BX+BY+BZ+VXM+VYM+VZM+-VNX(1D)+VNY(1D)+VNZ(1D))
                                                                                  0159
      DANG=ARCOS (SPRD)
                                                                                  0160
                                                                                  0161
      S1GN=1 .
      1F(BY.LT.O.) S1GN=-1.
                                                                                  0162
      PS1L=P12+S1GN*DANG
                                                                                  0163
      GO TO 310
                                                                                  0164
  309 CONTINUE
                                                                                  0165
      CALL FNORM(FIX, FTY, FTZ, RW, THTW, O.)
                                                                                  0166
      SPRD=VXM*FTX+VYM*FTY+VZM*FTZ
                                                                                  0167
      CALL CROSS(BX+BY+BZ+VXM+VYM+VZM+FTX+FTY+FTZ)
                                                                                  0168
                                                                                  0169
      DANG=ARCOS (SPRD)
                                                                                  0170
      S1GN=1 .
      1F(BY.LT.0.) S1GN=-1.
                                                                                  0171
                                                                                  0172
      PSIU=PI2+SIGN*DANG
      SPRD=-VXM*FTX+VYM*FTY+VZM*FTZ
                                                                                  0173
      DANG=ARCOS(SPRD)
                                                                                  0174
                                                                                  0175
      PSIL=PIZ-DANG
  310 CONTINUE
                                                                                  0176
      WRITE(6.15)PS1U.PSIL
                                                                                  0177
      DETERMINE PHASE OF WEDGE
                                                                                  0178
C
      PHWU=PHASE (THT.O., THTW.O., RW.FK)
                                                                                  0179
      PHWL=PHASE (THT . O . . THT x . P1 . RW . FK)
                                                                                  0180
                                                                                  0181
      PSUP=2.*PS1U
                                                                                  0182
      PSUM=U.
      PSLP=2.*PSIL
                                                                                  0183
                                                                                  0184
      PSI M= 0.
      BESSLO TEST
                                                                                  0185
C
      STT0=3.8317/BESAR
                                                                                  0186
      STT1=SIN(THT)
                                                                                  0187
                                                                                  0188
      WRITE (6.13) STT1
                                                                                  0189
      IF (STTI.LT.STTO)GO TO 302
                                                                                  0190
C
      SIN(X)/X TEST
                                                                                  0191
      1DX = 1D
```

```
T_1 = ABS(THSX(1DX) - THT)
                                                                               0192
      IF(T1.GT.P12) T1=P12
                                                                               0193
      ARSX=2.*FK*FLSX(1DX)*SIN(T1)
                                                                               0194
                                                                               0195
      WR1TE(6,14)ARSX
      1F(ARSX.LT.P1)GOTO 304
                                                                               0196
 303 CONTINUE
                                                                               0197
      NCHECK=303
                                                                               0198
      WRITE(6.1) NCHECK
                                                                               0199
      1F(1D.EO.1) GO TO 305
                                                                               0200
      CALCULATE DIFFRACTED FIELDS
                                                                               0201
C
      WDU=D1FF1(FN(1D),PSUP,FK,P12)+POL*D1FF1(FN(1D),PSUM,FK,P12)
                                                                               0202
      1F(1D.EO.1DSX) WDU=(0..C.)
                                                                               0203
      WDL=DIFF1(FN(1D),PSLP,FK,PI2)+POL*D1FF1(FN(1D),PSLM,FK,P12)
                                                                               0204
      RDF=SQRT(ABS(AW/(2.*SIN(THT))))
                                                                               0205
      WRITE(6.7) WDU, WDL, RDF
                                                                               0206
      EDU=RDF*PH#U*WDU*FW1U
                                                                               0207
      EDL=RDF*PHWL*WDL*FWIL
                                                                               0208
                                                                               0209
      EDTOT=EDTOT+EDU+EDL
      GO TO 301
                                                                               0210
     CONTINUE
                                                                               0211
 304
      NCHECK=304
                                                                               0212
      WRITE(6+1) NCHECK
                                                                               0213
      COMPUTE SIN(X)/X CONTRIBUTION
C
                                                                               0214
      COMPUTE PEAK RETURN USING AVERAGE OF GAUSSIAN CURVATURE
                                                                               0215
                                                                               0216
      RW1=RW
      RW2=RAD(THTF(1D))
                                                                               0217
      AW1 = AW
                                                                               0218
                                                                               0219
      AW2=RW2*SIN(THTF(ID))
                                                                               0220
      TAW=ABS(AW1-AW2)
      1F(TAW.LT.0.1) GO TO 307
                                                                               0221
                                                                               0222
      RH1=AW1/SIN(THT)
                                                                               0223
      RH2=AW2/SIN(THT)
                                                                               0224
      RH1 = ABS(RH1)
                                                                               0225
      RH2=ABS(RH2)
                                                                               0226
      RSH1=SORT (RHI)
                                                                               0227
      RSH2=SQRT(RH2)
      PEAK=ABS(RSH1*RH1-RSH2*RH2)*FLSX(1D)*I.414/(3.*ABS(RH1-RH2))
                                                                               0228
                                                                               0229
      PEAK=FK*PEAK
      GO TO 308
                                                                               0230
 307 PEAK=SGRT(AW1/2.)*FK*FLSX(1D)
                                                                               0231
                                                                               0232
 308 CONTINUE
                                                                               0233
      ESX=-PEAK*SINXX(ARSX)/SORT(TP*FK)
                                                                               0234
      ESX=ESX*PHASE(THT.O. THTW.O. RW.FK)
                                                                               0235
      1DSX=1D+I
      WRITE(6.11)THTD.ESX
                                                                               0236
                                                                               0237
      EDTOT=EDTOT+ESX
                                                                               0238
      GO TO 301
                                                                                0239
 302 CONTINUE
                                                                                0240
      NCHECK=302
                                                                                0241
      WRITE(6+1) NCHECK
                                                                               0242
      COMPUTE FIELD USING BESSEL FUNCTIONS
C
                                                                               0243
      SBSS=0.5
                                                                               0244
      PKSPC=FK*AW*AW
                                                                                0245
      PKBSS=AW
                                                                                0246
      ARGBS=BESAR*SIN(THT)
                                                                                0247
      IF(ABS(ARGBS).GT.0.05) SBSS=dESL1(ARGBS)/ARGBS
                                                                                0248
      CALL FNORM(F1X.F1Y.FIZ.RW.THTW.O.)
                                                                                0249
      PSUB=2.*(P12-ARCOS(AHS(F1Z)))
      1F(THT.LT.PI2) PSUB=2.*(PI2-ARCOS(VNZ(ID)))
                                                                                0250
                                                                                0251
      WBS=DIFF1(FN(1D).PSUB.FK.P12)
                                                                                0252
      PBESS=PHASE(THT.0..0..0..ZW.FK)
                                                                                0253
      SHBDT=CABS(WBS)-0.5
      IF(ABS(SHBDT).LT.0.05) GO TO 321
                                                                                0254
                                                                                0255
      WAS=WBS*SORT(TP*FK)
```

```
COST=COS(THT)
                                                                                0256
     WBSP=DIFFI(FN(ID),0.,FK,PI2)+DIFFI(FN(ID),PSUB,FK,PI2)
                                                                                0257
     WBSM=DIFFI(FN(ID),0.,FK,PI2)-DIFFI(FN(ID),PSUB,FK,PI2)
                                                                                0258
     WBSP=WBSP*SQRT(FK*TP)
                                                                                0259
     WBSM=WBSM*SQRT(TP*FK)
                                                                                0260
     WBS=-COST*COST*WBSM*SBSS+WBSP*(SBSS-BESL2(ARGBS))
                                                                                0261
      IF(POL.LT.O.) WBS=COST*COST*WBSP*SBSS-WBSM*(SBSS-BESL2(ARGBS))
                                                                                0262
      EBESS=(0.,-I.)*PKBSS*PBESS*WBS
                                                                                0263
      IF (FWIU.EQ.O..AND.FWIL.EQ.O.) EBESS = (0..O.)
                                                                                0264
      IF (FWIU.GT.J..AND.FWIL.EQ.O.) EBESS=0.5*EBESS
                                                                                0265
      GO TO 322
                                                                                0266
  321 CONTINUE
                                                                                0267
      EBESS=(0.+-1.)*PKSPC*PBESS*SBSS
                                                                                0268
  322 CONTINUE
                                                                               0269
      WRITE(6.12) THTD. EBESS
                                                                                0270
     EDTOT=EDTOT+FBESS
                                                                               0271
     GO TO 301
                                                                               0272
     CONTINUE
 305
                                                                               0273
     NCHECK=305
                                                                               0274
      WRITE(6.1) NCHECK
                                                                               0275
      COMPUTE TIP CONTRIBUTION AT ENDS
C
                                                                               0276
      TO FIRST ORDER TIP CONTRIBUTIONS ARE NEGLEGIBLE
C
                                                                               0277
      THTCN=THT
                                                                               0278
      IF (THT . GT . PI2) THTCN=PI-THT
                                                                               0279
     HFCA=0.5*WA(ID)
                                                                               0280
      TCNA=PI2-HFCA
                                                                               0281
      TCNAA=ABS(THTCN-TCNA)
                                                                               0282
      IF(TCNAA.LT.0.1745) GO TO 312
                                                                               0283
     IF(ABS(HFCA-PI2).LT.0.1745) GO TO 312
                                                                               0284
     TANA=TAN(HFCA)
                                                                               0285
      TANA2=TANA*TANA
                                                                               0286
      TANTHETAN (THICK)
                                                                               0287
      TANT2=TANTH*TANTH
                                                                               0288
      COSTH=COS(THCN)
                                                                               0289
      COSTH3=COSTH*COSTH*COSTH
                                                                               0290
      ETIP=-WAVE*TANA2/(8.*PI*COSTH3*(I.-TANA2*TANT2))
                                                                               0291
      ETIP=ETIP*PHASE(THT.O..O..O..ZW.FK)
                                                                               0292
      IF (POL.LT.O.) ETIP=-ETIP
                                                                               0293
      GO TO 311
                                                                               0294
  312 ETIP=(0..0.)
                                                                               0295
  311 CONTINUE
                                                                               0296
      FDTOT=FDTOT+FTIP
                                                                               0297
                                                                               0298
 30 I
    CONTINUE
                                                                               0299
      OUTPUT SECTION
С
      WRITE(6.4) THTD.EDTOT
                                                                               0300
      EMAG=CABS (EDTOT)
                                                                                030 I
      SIGMA=2.*TP*EMAG*EMAG/(WAVE*WAVE)
                                                                               0302
      SIGMAL=10.*ALOGIO(SIGMA)
                                                                               0303
      WRITE(6.4)SIGMA.SIGMAL
                                                                               0304
 400 CONTINUE
                                                                               0305
  600 CONTINUE
                                                                               0306
      STOP
                                                                               0307
                                                                               0308
     END
                                                                               0309
$IBFTC FFNRM
             LIST . NODECK
      SUBROUTINE FNORM(FNVX.FNVY.FNVZ.R.THT.PHI)
                                                                               0310
                                                                               0311
      INPUT R.THT.PHI
C
      COMMON ARI+AR3+BR1+AR9+ARIO+ARII
                                                                               0312
                                                                               0313
      ST=SIN(THT)
      CT=(OS(THT)
                                                                               0314
                                                                               0315
      SP=SIN(PHI)
                                                                               0316
      CP=COS(PHI)
      U=ARI*ST*ST+AR3*CT*CT+BRI*ST*CT
                                                                               0317
      V=AR9*CT+ARI0*ST
                                                                               0318
      UTH=2.*(ARI-AR3)*ST*CT+BRI*(CT*CT-ST*ST)
                                                                               0319
```

```
VTH=-AR9*ST+AR10*CT
                                                                                     0320
      F1=2.*R*U+V
                                                                                     0321
      F2=R*UTH+VTH
                                                                                     0322
      FX=ST*CP*F1+CT*CP*F2
                                                                                     0323
      FY=ST*SP*F1+CT*SP*F2
                                                                                     0324
      FZ=CT*F1-ST*F2
                                                                                     0325
      FN=SQRT(FX*FX+FY*FY+FZ*FZ)
                                                                                     0326
      FNVX=FX/FN
                                                                                     0327
      FNVY=FY/FN
                                                                                     0328
      FNVZ=FZ/FN
                                                                                     0329
      RETURN
                                                                                     0330
      END
                                                                                     0331
SIBFTC FCOMM. LIST.NODECK
                                                                                     0332
      SUBROUTINE FCOMM(I)
                                                                                     0333
      COMMON RA1, RA3, RB1, RA9, RA10, RA11/DATA/AR1(20), AR3(20), BR1(20), AR9(
                                                                                     0334
     C20) + AR10(2J) + AR11(20)
                                                                                     0335
      RAI = ARI(I)
                                                                                     0336
      RA3=AR3(1)
                                                                                     0337
      RB1=BR1(I)
                                                                                     0338
      RA9=AR9(1)
                                                                                     0339
      RAID=AR10(I)
                                                                                     0340
      RA1I = ARII(I)
                                                                                     0341
      RETURN
                                                                                     0342
      END
                                                                                     0343
SIBFIC RADD
               LIST , NODECK
                                                                                     0344
      FUNCTION RAD(THT)
                                                                                     0345
      CALCULATE R
                                                                                     0346
C
      COMMON ARI . AR3 . BRI . AR9 . AR10 . AR11
                                                                                     0347
      R=0.
                                                                                     0348
                                                                                     0349
      ST=SIN(THT)
      CT=COS(THT)
                                                                                     0350
      C1=AR1*ST*ST+AR3*CT*CT+BR1*ST*CT
                                                                                     0351
      C2=AR9*CT+AR10*ST
                                                                                     0352
      C3=AR11
                                                                                     0353
      IF (C1 . EQ . O . ) GO TO II
                                                                                     0354
      ARG=SQRT(C2*C2-4.*C1*C3)
                                                                                     0355
      R = (-C2 + ARG) / (2.*C1)
                                                                                     0356
      R2 = (-C2 - ARG)/(2 \cdot *C1)
                                                                                     0357
                                                                                     0358
      IF (R2.LT.R.AND.R2.GT.O.) R=R2
                                                                                     0359
      GO TO 12
      R=-C3/C2
                                                                                     0360
 11
                                                                                     0361
      RAD=ABS(R)
 12
                                                                                     0362
      RETURN
                                                                                     0363
      END
                                                                                     0364
SIBFTC WILLY. LIST.NODECK
      SUBROUTINE WILLY (FWI . THTI . PHI . THIN . PHIN)
                                                                                     0365
      INPUT THTI.PHI.THIN.PHIN
                                                                                     0366
C
                                                                                     0367
      FWI=0. WEDGE IN SHADOW
C
                                                                                     0368
                WEDGE ILLUMINATED
C
      F W I = 1 .
                                                                                     0369
      COMMON ARI . AR3 . BRI . AR9 . ARIC . ARII
                                                                                     0370
      PI=3.1415927
                                                                                     0371
      PI2=I . 5707963
                                                                                     0372
      (ITHT) CASES
                                                                                     0373
      CALL FNORM (FNX, FNY, FNZ, R, THTI, PHI)
                                                                                     0374
      TH=THIN
                                                                                     0375
      XIN=SIN(TH)*COS(PHIN)
                                                                                     0376
      YIN=0.
                                                                                     0377
      ZIN=COS(TH)
                                                                                     0378
      SPRD=FNX*XIN+FNY*YIN+FNZ*ZIN
                                                                                     0379
      FWI = 1 .
                                                                                     0380
      IF (SPRD.LT.O.) FWI=O.
                                                                                     0381
      CONTINUE
                                                                                     0382
      RETURN
                                                                                     0383
      END
```

```
$IBFTC CROSS. LIST.NODECK
                                                                                                                                                                                                   0384
                 SUBROUTINE CROSS(X+Y+Z+AI+A2+A3+B1+B2+B3)
                                                                                                                                                                                                   0385
               X=A2*B3-A3*B2
                                                                                                                                                                                                   0386
               Y=A3*B1-A1*B3
                                                                                                                                                                                                  0387
               Z=A1*B2-A2*BI
                                                                                                                                                                                                  0388
              RETURN
                                                                                                                                                                                                  0389
              END
                                                                                                                                                                                                  0390
$IBFTC PHAS.
                                     LIST . NODECK
                                                                                                                                                                                                  0391
                 COMPLEX FUNCTION PHASE (THT1,PHII,THTB,PHIB,RB,FK)
                                                                                                                                                                                                  0392
                                                                                                                                                                                                  0393
               TEST=ABS(PHII-PHIB)
                                                                                                                                                                                                  0394
               IF (TEST.EQ.J.) FS=-I.
                                                                                                                                                                                                  0395
              FL=2.*RB*COS(THTI+FS*THTB)
                                                                                                                                                                                                  0396
              FKL=FK*FL
                                                                                                                                                                                                  0397
              PHASE=CMPLX(COS(FKL) +SIN(FKL))
                                                                                                                                                                                                  0398
                 RETURN
                                                                                                                                                                                                  0399
              END
                                                                                                                                                                                                  0400
$IBFTC SINXX. LIST.NODECK
                                                                                                                                                                                                  0401
              FUNCTIONSINXX(Y)
                                                                                                                                                                                                  0402
               SIN(X)/X FUNCTION
                                                                                                                                                                                                  0403
               7 = Y * Y
                                                                                                                                                                                                  0404
               SINXX = (I - -(Z/6 - )*(I - -(Z/20 - )*(I - -(Z/42 - )*(I - -(Z/72 - )*(I - -(Z/110 - )*(
                                                                                                                                                                                                  0405
             2(1 \bullet - (Z/156 \bullet) * (1 \bullet - (Z/182 \bullet))))))))
                                                                                                                                                                                                  0406
               RF TURN
                                                                                                                                                                                                  0407
              FND
                                                                                                                                                                                                  0408
$IBFTC DIFCN
                                     LIST . NODECK
                                                                                                                                                                                                  0409
               COMPLEX FUNCTION DIFF1 (FN+PHI+FK+BETA)
                                                                                                                                                                                                  0410
               SINGLE DIFFRACTION FUNCTION DIFFI
C
                                                                                                                                                                                                  0411
               FN-WEDGE ANGLE, PHI=ARGUMENT, BETA=CONE ANGLE
C
                                                                                                                                                                                                  0412
               COMPLEX EXPH
                                                                                                                                                                                                  0413
               PI=3.1415927
                                                                                                                                                                                                  0414
               TP=2.*PI
                                                                                                                                                                                                  0415
               PI4=PI/4.
                                                                                                                                                                                                  0416
               PIF=PI/FN
                                                                                                                                                                                                  0417
               PHN=PHI/FN
                                                                                                                                                                                                  0418
              PHIA=ABS(PHI)
                                                                                                                                                                                                  0419
              EXPH=CEXP((0.+-1.)*PI4)
                                                                                                                                                                                                  0420
               SINB=SIN(BETA)
                                                                                                                                                                                                  0421
               SINB=ABS(SINB)
                                                                                                                                                                                                  0422
               IF(SINB.LT..OOI) GO TO 3
                                                                                                                                                                                                  0423
               IF (ABS(PHIA-PI).LT.O.I) GO TO I
                                                                                                                                                                                                  0424
               T1 = COS(PIF)
                                                                                                                                                                                                  0425
               T2=COS (PHN)
                                                                                                                                                                                                  0426
               T3=SIN(PIF)
                                                                                                                                                                                                  0427
               T4=T1-T2
                                                                                                                                                                                                  0428
               T4A=ABS(T4)
                                                                                                                                                                                                  0429
               IF(T4A.LT..JJI) GO TO 3
                                                                                                                                                                                                  0430
               DIFFI=EXPH*T3/(FN*SINB*T4)
                                                                                                                                                                                                  0431
               DIFFI=DIFFI/SQRT(TP*FK)
                                                                                                                                                                                                  0432
                                                                                                                                                                                                  0433
               GO TO 2
                                                                                                                                                                                                  0434
   I
               DIFFI=0.5/SINB
                                                                                                                                                                                                  0435
               GO TO 2
                                                                                                                                                                                                  0436
               DIFFI=1000J.
   3
               CONTINUE
                                                                                                                                                                                                  0437
  2
               RETURN
                                                                                                                                                                                                  0438
                                                                                                                                                                                                  0439
               END
$1BFTC BESLO. LIST.NODECK
                                                                                                                                                                                                  0440
               FUNCTION BESLO(X)
                                                                                                                                                                                                  0441
                                                                                                                                                                                                  0442
               (X.GT.O.)
C
                                                                                                                                                                                                  0443
               Z = ABS(X)
                                                                                                                                                                                                  0444
               Y=X/3.
                                                                                                                                                                                                  0445
               Y2=Y*Y
               Y3=Y2*Y
                                                                                                                                                                                                  0446
                                                                                                                                                                                                  0447
               Y4=Y2*Y2
```

```
Y5=Y3*Y2
                                                                                                                                                                                                                            0448
                Y6=Y4*Y2
                                                                                                                                                                                                                            0449
                Y8=Y6*Y2
                                                                                                                                                                                                                            0450
                Y10=Y8*Y2
                                                                                                                                                                                                                            0451
                Y12=Y10*Y2
                                                                                                                                                                                                                            0452
                IF (Z • GT • 3 • ) GO TO 10
                                                                                                                                                                                                                            0453
                8ESL0=1 -- 2 • 2499997*Y2+1 • 2656208*Y4- • 3163866*Y6+ • 0444479*Y8- • 003944
                                                                                                                                                                                                                            0454
              24*Y10-.00024846*Y12
                                                                                                                                                                                                                            0455
                GO TO 11
                                                                                                                                                                                                                            0456
  1.0
                CONTINUE
                                                                                                                                                                                                                            0457
                F=.79788456-(.00000077/Y)-(.00552740/Y3)-(.00009512/Y3)+(.00137237
                                                                                                                                                                                                                            0458
              2/44)-(.00072805/45)+(.00014476/46)
                                                                                                                                                                                                                            0459
                 T=X-.78539316-(.04156397/Y)-(.00003954/Y2)+(.00262573/Y3)-(.000541)
                                                                                                                                                                                                                            0460
              225/Y4)-(.00029333/Y5)+(.00013558/Y6)
                                                                                                                                                                                                                            0461
                8ESL0=F*COS(T)/SQRT(X)
                                                                                                                                                                                                                            0462
  1 I
                CONTINUE
                                                                                                                                                                                                                            0463
                RETURN
                                                                                                                                                                                                                            0464
                END
                                                                                                                                                                                                                            0465
$18FTC BESLI. LIST.NODECK
                                                                                                                                                                                                                            0466
                FUNCTION BESLI(X)
                                                                                                                                                                                                                            0467
                POLYNOMIAL APPROXIMATION X.GT.O.
C
                                                                                                                                                                                                                            0468
                Y = X/3
                                                                                                                                                                                                                            0469
                Y2=Y*Y
                                                                                                                                                                                                                            0470
                 Y3=Y2*Y
                                                                                                                                                                                                                            0471
                 Y4=Y3*Y
                                                                                                                                                                                                                            0472
                 Y5=Y4*Y
                                                                                                                                                                                                                            0473
                 Y6=Y5*Y
                                                                                                                                                                                                                            0474
                 Y8=Y6*Y2
                                                                                                                                                                                                                            0475
                 Y10=Y8*Y2
                                                                                                                                                                                                                            0476
                 Y12=Y10*Y2
                                                                                                                                                                                                                            0477
                 IF(X.GT.3.)GO TO 10
                                                                                                                                                                                                                            0478
                BESL=0.5-.56249985*Y2+.21093573*Y4-.03954289*Y6+.00443319*Y8-.0003
                                                                                                                                                                                                                            0479
              21761*Y10+.00001109*Y12
                                                                                                                                                                                                                            0480
                                                                                                                                                                                                                            0481
                BESL1=X*8ESL
                GO TO 11
                                                                                                                                                                                                                            0482
                CONTINUE
                                                                                                                                                                                                                            0483
   10
                F=.79788456+(.00000156/Y)+(.01659667/Y2)+(.00017105/Y3)-(.00249511
                                                                                                                                                                                                                            0484
              2/44)+(.00113653/45)-(.00020033/46)
                                                                                                                                                                                                                            0485
                 T = X - 2 \cdot 35619449 + ( \cdot 12499612/Y ) + ( \cdot 00005650/Y2 ) - ( \cdot 00637879/Y3 ) + ( \cdot 00074849 + ( \cdot 12499612/Y ) + ( \cdot 00005650/Y2 ) - ( \cdot 00637879/Y3 ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 00005650/Y2 ) - ( \cdot 00637879/Y3 ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 00005650/Y2 ) - ( \cdot 00637879/Y3 ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 00005650/Y2 ) - ( \cdot 000637879/Y3 ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 000074849 + ( \cdot 12499612/Y ) + ( \cdot 0000074849 + 
                                                                                                                                                                                                                            0486
              2348/Y4)+(.00079824/Y5)-(.00029166/Y6)
                                                                                                                                                                                                                            0487
                8ESL1=F*COS(T)/SQRT(X)
                                                                                                                                                                                                                            0488
                CONTINUE
                                                                                                                                                                                                                            0489
  1 1
                                                                                                                                                                                                                            0490
                RETURN
                                                                                                                                                                                                                            0491
                FND
                                                                                                                                                                                                                            0492
$IBFTC BESL2. LIST.NODECK
                 FUNCTION BESL2(X)
                                                                                                                                                                                                                            0493
C
                 (X.GT.J.)
                                                                                                                                                                                                                            0494
                 IF(X.EQ.0.)GO TO 10
                                                                                                                                                                                                                            0495
                                                                                                                                                                                                                            0496
                 BFSL2=(2.*BESL1(X)/X)-BESL0(X)
                                                                                                                                                                                                                            0497
                 GO TO 11
                                                                                                                                                                                                                            0498
   10
                 BESL2=0.
                                                                                                                                                                                                                            0499
                 CONTINUE
   11
                                                                                                                                                                                                                            0500
                 RETURN
                                                                                                                                                                                                                            0501
                 END
                                                                                                                                                                                                                            0502
BDATA
```

APPENDIX II INPUT DATA

00002 00003 1.0 0. .785398 2.617	0. .785398 2.617 3.1415927	180. 0. 0.	1.0 0. 0.	-1. 0. 0.	2.0 0. -1.0	1.0 1.0 0	-2.0 -1.0 -2.0
00003 1.0 0. .785398 2.617	0. .785398 2.617 3.1415927	180. 0. 0.	1.0 0. 0.	1.0 0. 0.	2.0 0. -1.0	1.0 1.0 0.	-2.0 -1.0 -2.0

APPENDIX III COMPUTER TESTS FOR E_{φ} POLARIZATION

A limited amount of data has been obtained for the case of Ed polarization. The computed results are compared with measured data for the cone and double cone in Figs. 3 and 4. The data for the cone is that of Keys and Primich⁵ and the double cone data is from Eberle and St. Clair. 6 For the case of the cone the greatest error is in the near forward region where the single diffraction solution is used. The results in this region agree with the single diffraction results of Bechtel. The results in this region could be improved by extending the edge current formulation for the axially scattered fields to this region. In the case of the double cone the calculated echo area is in error in the region about $\theta = 90^{\circ}$. This is a region where the effect of edge type creeping waves at the junction should be considered. These test results indicate that further extension of the theory and computer program is necessary to remove these sources of error. However, for targets which are large in terms of wavelength the accuracy will improve, as both the edge current and creeping wave effects would diminish.

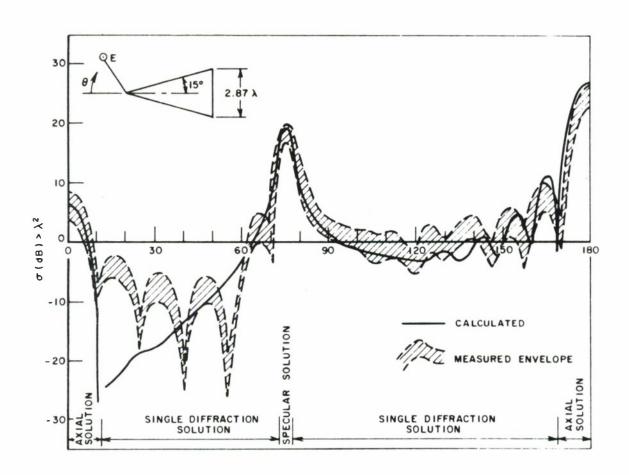


Fig. 3. Echo area of a cone- $\boldsymbol{E}_{\!\varphi}$ polarization.

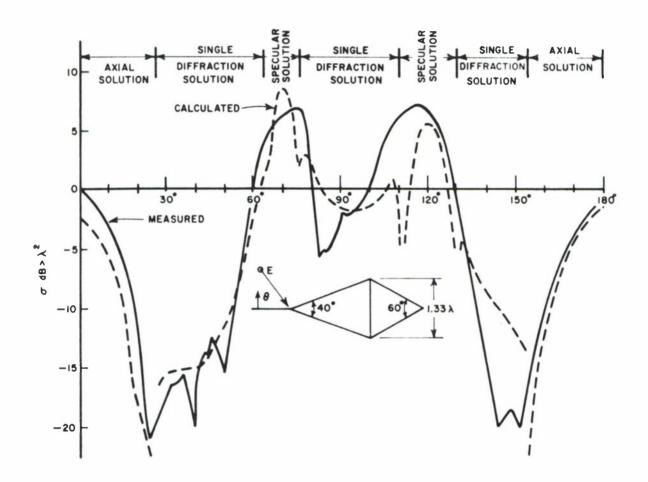
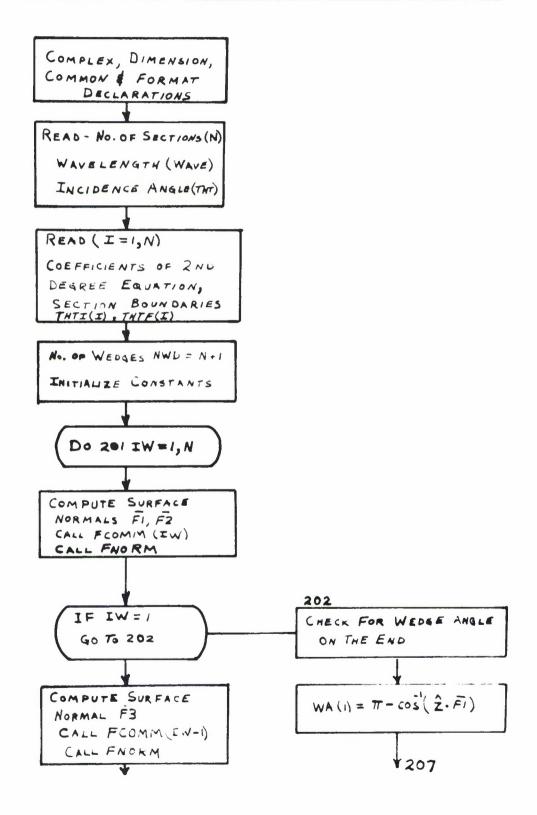


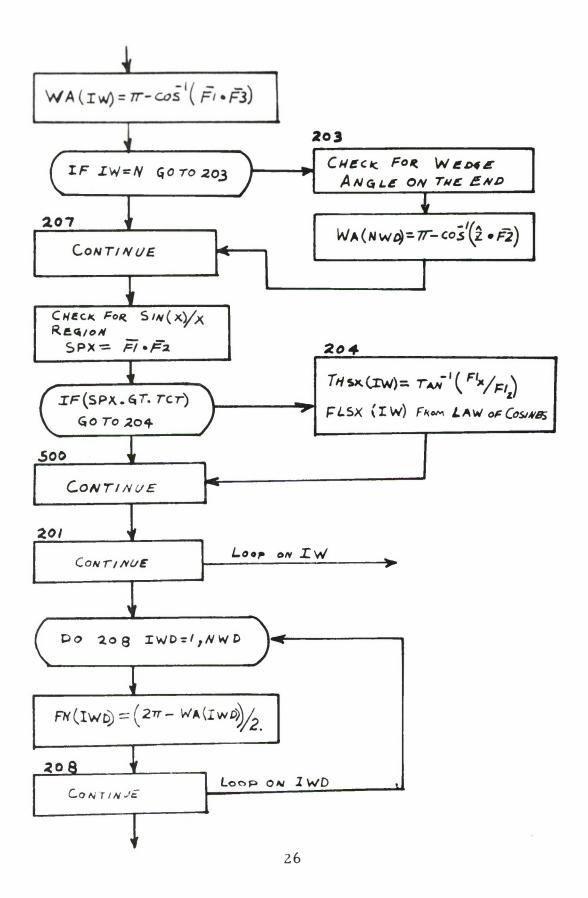
Fig. 4. Echo area of a double cone-E $_{\varphi}$ polarization.

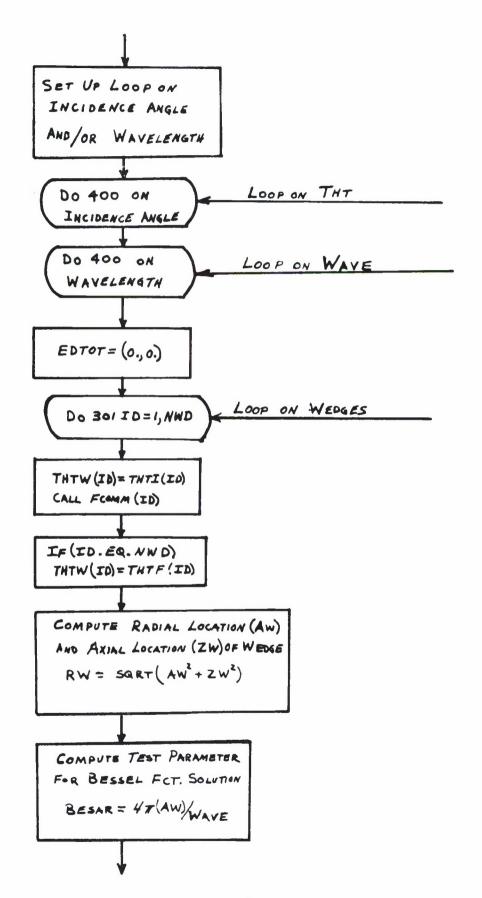
APPENDIX IV WEDGE DIFFRACTION COMPUTER PROGRAM FLOW DIAGRAM

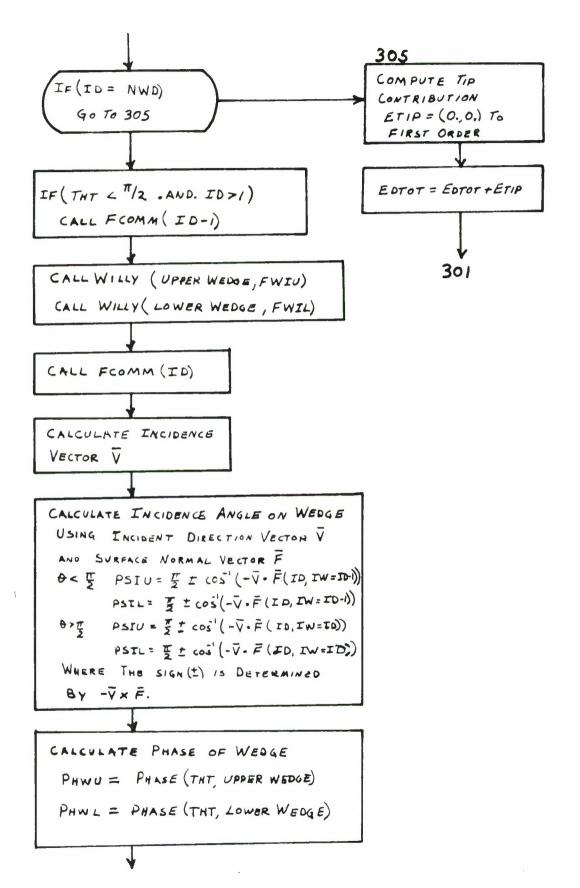
The flow diagram for the wedge diffraction Computer program WEDGD is given in Fig. 5. This flow diagram has also been presented in Ref. 1.

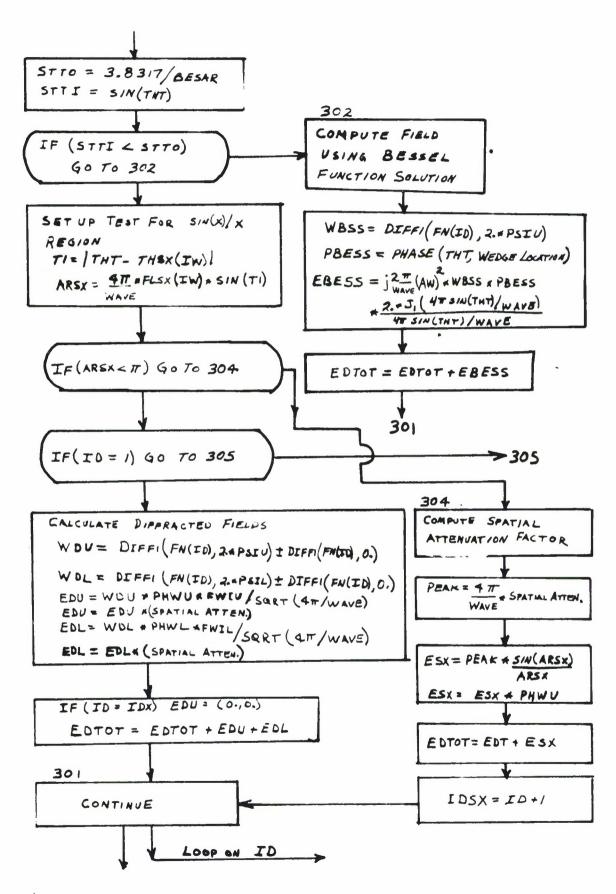
WEDGE DIFFRACTION COMPUTER PROGRAM

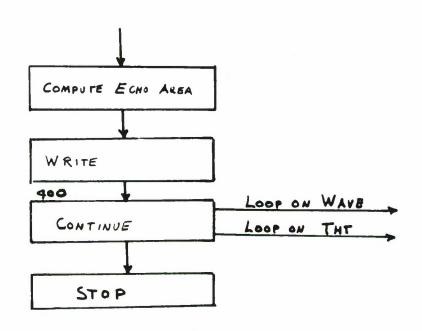












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This report describes a computer program for determining the back-					
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cones and cylinders. The target may be closed at one or both ends with					
circular disks. The target may have as many as 20 sections, and the					
program can readily be modified to handle a larger number. The back-					
scattered field for E_{θ} or E_{ϕ} polarization is computed using wedge diffraction					
theory and geometrical optics. The computed results are in good agree-					
ment with experimental measurements for cones, cylinders, double cones,					

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and conically capped cylinders.

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